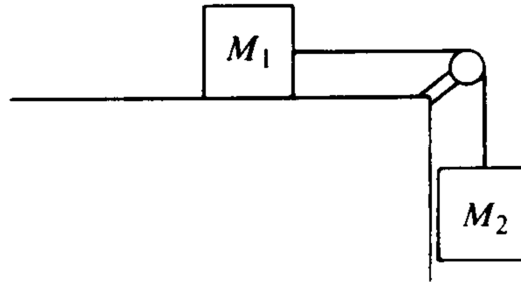


LINEAR MOMENTUM PRACTICE

For each question, please highlight/underline the important information given, and then organize your answers into coherent statements that are backed by equation-based evidence. You will need to identify and rearrange formulas to determine the correct answers.

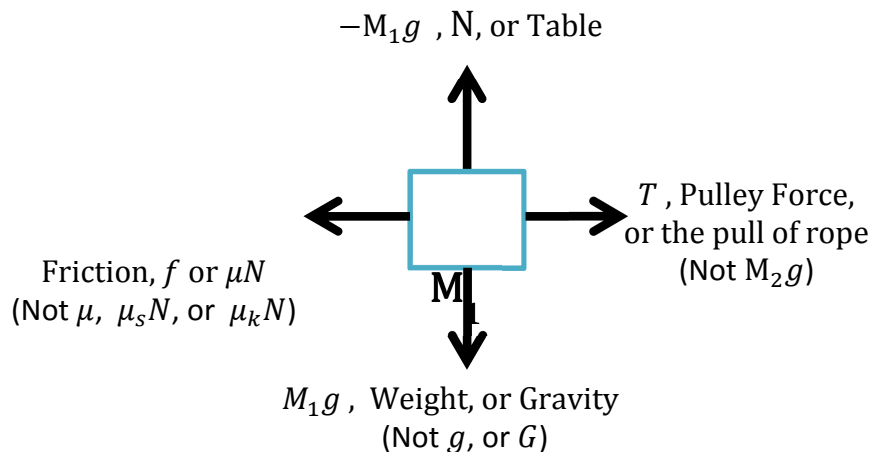
[1987B1.]

- LINEAR MOMENTUM



In the system shown above, the block of mass M_1 is on a rough horizontal table. The string that attaches it to the block of mass M_2 passes over a frictionless pulley of negligible mass. The coefficient of kinetic friction μ_k between M_1 and the table is less than the coefficient of static friction μ_s .

a.) On the diagram below, draw and identify all the forces acting on the block of mass M_1 .



b.) In terms of M_1 and M_2 determine the minimum value of μ_s that will prevent the blocks from moving.

- Start with the Main Force Equation: $\sum F_{External} = m_{Total} \cdot a$
- The maximum force of static friction on mass M_1 is $(\mu_s \cdot N)$
- And Normal Force for M_1 is $N = (M_1 \cdot g)$
- $M_2 \cdot g - \mu_s \cdot M_1 \cdot g = 0$
- Reduces to $\mu_s = \frac{M_2}{M_1}$

The blocks are set in motion by giving M_2 a momentary downward push. In terms of M_1 , M_2 , μ_k , and g , determine each of the following:

c.) The magnitude of the acceleration of M_1

- Start with the Main Force Equation: $\sum F_{External} = m_{Total} \cdot a$

- Now Kinetic Friction is acting on M_2 and the formula becomes

$$(M_2 \cdot g - \mu_k \cdot M_1 \cdot g) = (M_1 + M_2) \cdot a$$

- Rearrange the formula to solve for a

$$a = \frac{(M_2 \cdot g - \mu_k \cdot M_1 \cdot g)}{(M_1 + M_2)}$$

d.) The tension in the string.

- Start with the Main Force Equation: $\sum F_{External} = m_{Total} \cdot a$

- For the hanging block becomes the formula

$$(M_2 \cdot g - T) = (M_2 \cdot a)$$

- Substitute a from the above equation in part (c.)

$$(M_2 \cdot g) - T = \left[M_2 \cdot \left(\frac{(M_2 \cdot g) - \mu_k \cdot M_1 \cdot g}{(M_1 + M_2)} \right) \right]$$

- Now it's time to rearrange & solve for T

- Cancel from the above equation in part

$$\cancel{(M_2 \cdot g)} - T = \left[M_2 \cdot \left(\frac{(\cancel{M_2 \cdot g}) - (\cancel{M_2 \cdot g}) - \mu_k \cdot M_1 \cdot g}{(M_1 + M_2)} \right) \right]$$

$$-(M_2 \cdot g)$$

- Divide $-T$ by -1 to isolate $(-\mu_k)$ & turn the entire equation into

$$\frac{(-T)}{(-1)} = \left[M_2 \cdot \left(\frac{(-\mu_k) \cdot M_1 \cdot g}{(M_1 + M_2)} \right) \right] \frac{(-1)}{(-1)}$$

- This gives you a reduced answer of $T = \frac{M_2 \cdot M_1 \cdot g}{(M_1 + M_1)} (1 + \mu_k)$